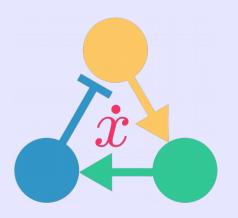




## Modelling chemical kinetics

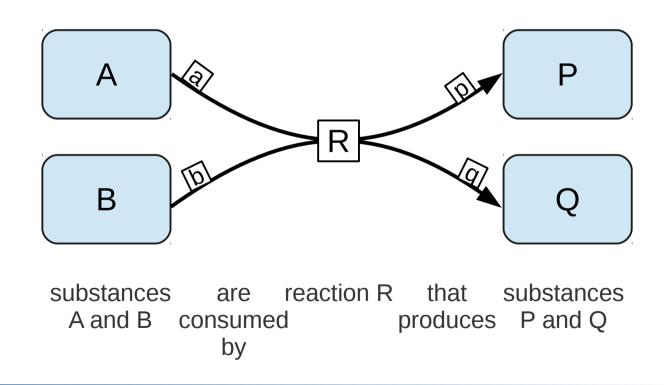
Nicolas Le Novère, Babraham Institute, EMBL-EBI

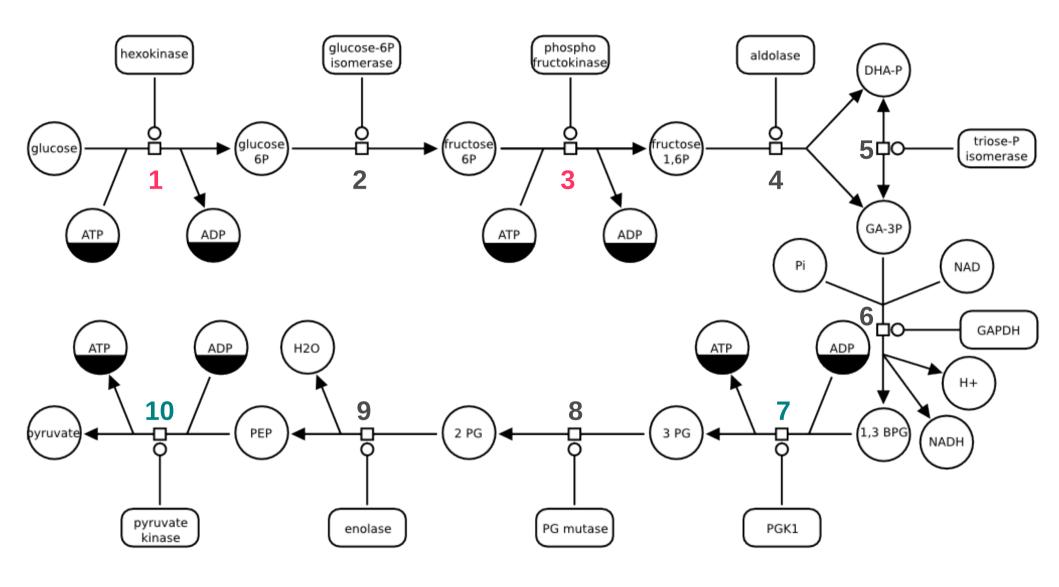
n.lenovere@gmail.com



## **Systems Biology models** ≠ ODE models

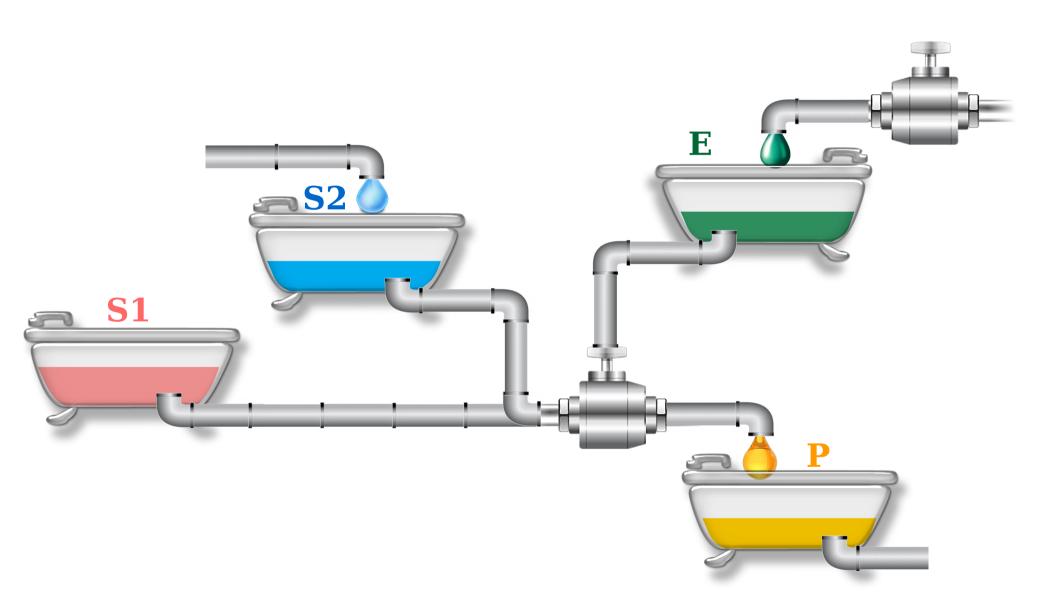
- → Reconstruction of state variable evolution from process descriptions:
- Processes can be combined in ODEs (for deterministic simulations);
   transformed in propensities (for stochastic simulations)
- Systems can be reconfigured quickly by adding or removing a process



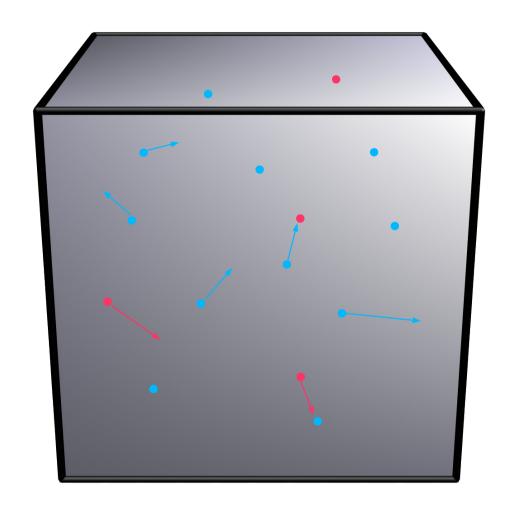


ATP is consumed by processes 1 and 3, and produced by processes 7 and 10 (for 1 reactions 1 and 3, there are 2 reactions 7 and 10)

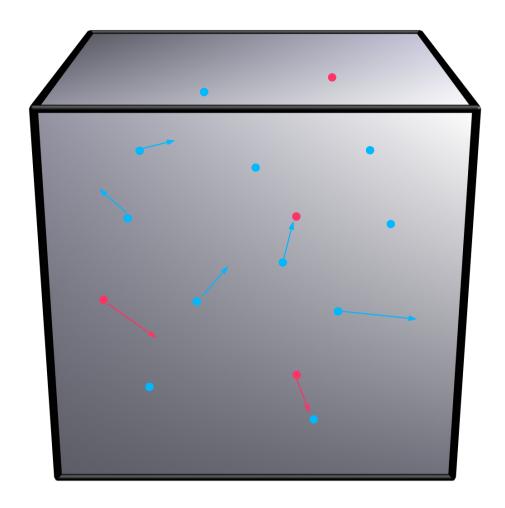
#### **Chemical kinetics and fluxes**



## Statistical physics and chemical reaction



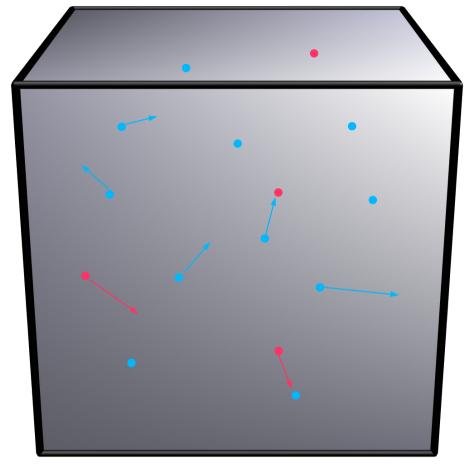
## Statistical physics and chemical reaction



Probability to find an object in a container within an interval of time

$$P(\bullet) \propto \frac{n(\bullet)}{V} = [\bullet]$$

## Statistical physics and chemical reaction



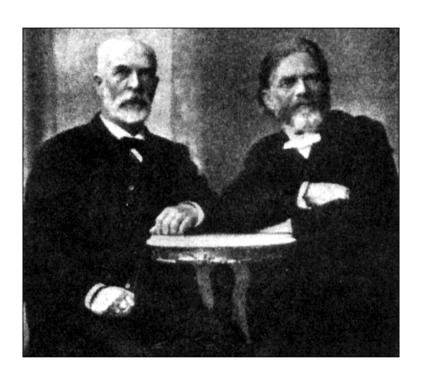
Probability to find an object in a container within an interval of time

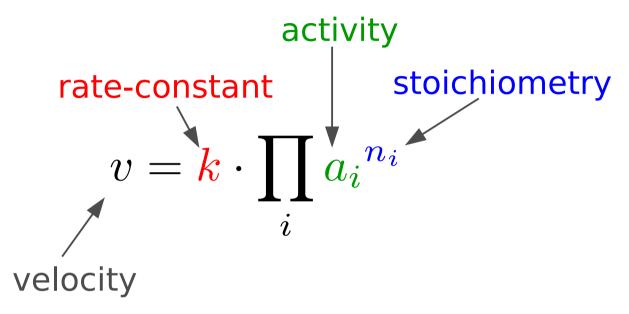
$$P(\cdot) \propto \frac{n(\cdot)}{V} = [\cdot]$$

$$P(\text{reaction } \bullet) = P(\bullet) \times P(\bullet \text{reacts})$$
  
 $P(\text{reaction } \bullet + \bullet) = P(\bullet) \times P(\bullet) \times P(\bullet \text{reacts with } \bullet)$   
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#### **Law of Mass Action**

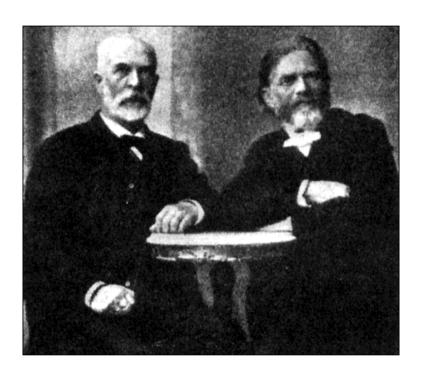
Waage and Guldberg (1864)

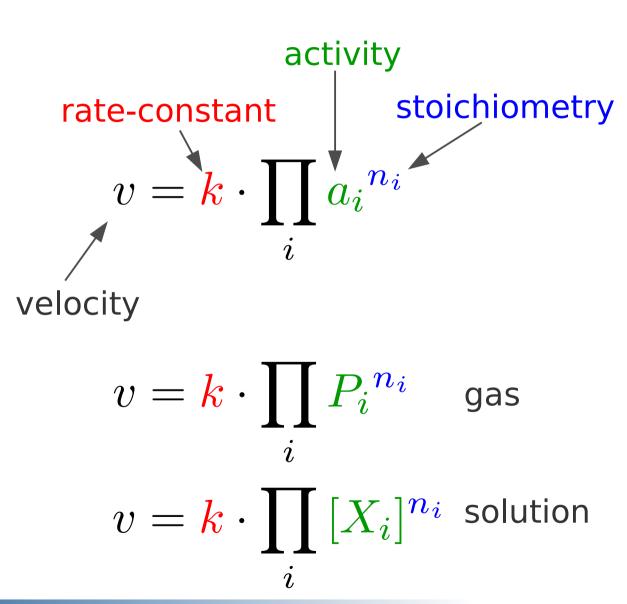




#### **Law of Mass Action**

Waage and Guldberg (1864)





#### **Evolution of a reactant**

- Velocity multiplied by stoichiometry
- negative if consumption, positive if production
- lacksquare Example of a unimolecular reaction  $x \stackrel{k}{
  ightarrow} y$

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- Example of a unimolecular reaction  $x \stackrel{k}{\rightarrow} y$

$$\frac{d[x]}{dt} = -1 \cdot v = -1 \cdot k \cdot [x]$$

$$\frac{d[y]}{dt} = +1 \cdot v = +1 \cdot k \cdot [x]$$

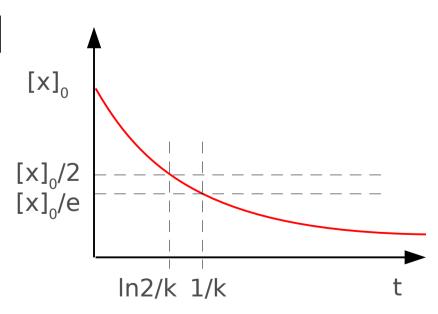
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$$x(t) = [x]_0 \cdot e^{-kt}$$



#### **Reversible reaction**

$$2x \stackrel{k1}{\rightleftharpoons} y$$
 is equivalent to  $2x 
ightarrow y; v1 = k1 \cdot [x]^2$   $y 
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#### **Reversible reaction**

$$2x \stackrel{k1}{\rightleftharpoons} y$$
 is equivalent to  $2x \to y; v1 = k1 \cdot [x]^2$   $y \to 2x; v2 = k2 \cdot [y]$ 

$$\frac{d[x]}{dt} = -2 \cdot v1 + 2 \cdot v2 = -2 \cdot k1 \cdot [x]^2 + 2 \cdot k2 \cdot [y]$$

$$\frac{d[y]}{dt} = +1 \cdot v1 - 1 \cdot v2 = +1 \cdot k1 \cdot [x]^{2} - 1 \cdot k2 \cdot [y]$$

$$E + S \stackrel{k_1}{\rightleftharpoons} ES \stackrel{k_3}{\Rightarrow} E + P$$

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$$d[E]/dt = -k_1[E][S] + k_2[ES] + k_3[ES]$$

$$d[S]/dt = -k_1[E][S] + k_2[ES]$$

$$d[ES]/dt = +k_1[E][S] - k_2[ES] - k_3[ES]$$

$$d[P]/dt = +k_3[ES]$$

$$E + S \rightleftharpoons_{k_{2}} ES \stackrel{k_{3}}{\Longrightarrow} E + P$$

$$d[E]/dt = -k_{1}[E][S] + k_{2}[ES] + k_{3}[ES]$$

$$d[S]/dt = -k_{1}[E][S] + k_{2}[ES]$$

$$d[ES]/dt = +k_{1}[E][S] - k_{2}[ES] - k_{3}[ES]$$

$$d[P]/dt = +k_{3}[ES]$$

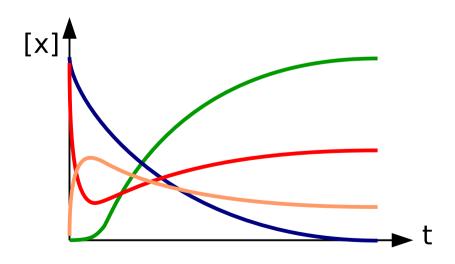
$$d[P]/dt = +k_{3}[ES]$$

$$\begin{pmatrix} d[E]/dt \\ d[S]/dt \\ d[ES]/dt \\ d[ES]/dt \\ d[P]/dt \end{pmatrix} = \begin{pmatrix} -1 & +1 & +1 \\ -1 & +1 & 0 \\ +1 & -1 & -1 \\ 0 & 0 & +1 \end{pmatrix} \times \begin{pmatrix} k_{1}[E][S] \\ k_{2}[ES] \\ k_{3}[ES] \end{pmatrix}$$

$$S = N \cdot v$$

$$E + S \stackrel{k_1}{\rightleftharpoons} ES \stackrel{k_3}{\Rightarrow} E + P$$

$$\begin{array}{rcl} d[E]/dt & = & -k_1[E][S] & +k_2[ES] & +k_3[ES] \\ d[S]/dt & = & -k_1[E][S] & +k_2[ES] \\ d[ES]/dt & = & +k_1[E][S] & -k_2[ES] & -k_3[ES] \\ d[P]/dt & = & & +k_3[ES] \end{array}$$



Not feasible in general

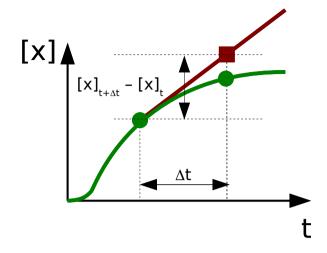
Numerical integration

## Numerical integration (only for info. Not needed)

#### **Euler method:**

$$d[x]/dt \approx ([x]_{t+\Delta t} - [x]_t)/\Delta t$$

$$[x]_{t+\Delta t} \approx [x]_t + d[x]/dt \cdot \Delta t$$



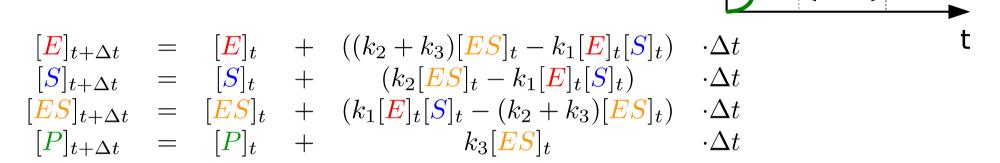
## Numerical integration (only for info. Not needed)

[x] **A** 

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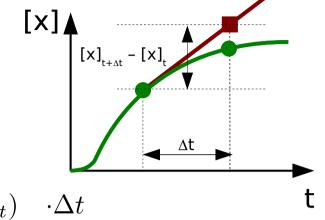


## Numerical integration (only for info. Not needed)

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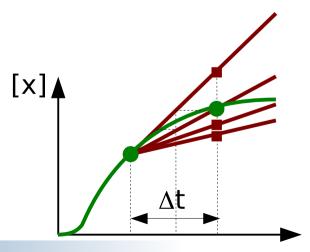
$$[x]_{t+\Delta t} \approx [x]_t + d[x]/dt \cdot \Delta t$$



$$\begin{aligned}
 [E]_{t+\Delta t} &= [E]_t + ((k_2 + k_3)[ES]_t - k_1[E]_t[S]_t) \cdot \Delta t \\
 [S]_{t+\Delta t} &= [S]_t + (k_2[ES]_t - k_1[E]_t[S]_t) \cdot \Delta t \\
 [ES]_{t+\Delta t} &= [ES]_t + (k_1[E]_t[S]_t - (k_2 + k_3)[ES]_t) \cdot \Delta t \\
 [P]_{t+\Delta t} &= [P]_t + k_3[ES]_t \cdot \Delta t
\end{aligned}$$

#### 4<sup>th</sup> order Runge-Kutta:

$$[x]_{t+\Delta t} \approx [x]_t + (F_1 + 2F_2 + 2F_3 + F_4)/6 \cdot \Delta t$$
 with 
$$F_1 = d[x]/dt = f([x]_t, t)$$
 
$$F_2 = f([x]_t + \Delta t/2 \cdot F_1, t + \Delta t/2)$$
 
$$F_3 = f([x]_t + \Delta t/2 \cdot F_2, t + \Delta t/2)$$
 
$$F_4 = f([x]_t + \Delta t \cdot F_3, t + \Delta t)$$



$$E + S \xrightarrow{k_{as}} ES \xrightarrow{k_{catp}} ES \xrightarrow{k_{catp}} EP \xrightarrow{k_{dp}} E + P \qquad \frac{d[P]}{dt} = k_{dp}[EP] - k_{ap}[E][P]$$

$$E + S \xrightarrow{k_{as}} ES \xrightarrow{k_{cats}} EP \xrightarrow{k_{dp}} E + P \qquad \frac{d[P]}{dt} = k_{dp}[EP] - k_{ap}[E][P]$$

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 irreversible catalysis

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 irreversible catalysis

$$E + S \xrightarrow{k_{as}} ES \xrightarrow{k_{cats}} E + P$$

product escapes before rebinding

$$S \xrightarrow{k_{cats}} P$$

quasi-steady-state

$$\frac{d[P]}{dt} = [E]k_{\text{cat}}\frac{[S]}{K_m + [S]}$$

## **Enzyme kinetics**

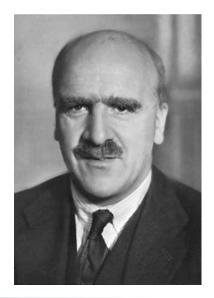
Victor Henri (1903) Lois Générales de l'Action des Diastases. Paris, Hermann.

Leonor Michaelis, Maud Menten (1913). Die Kinetik der Invertinwirkung, Biochem. Z. 49:333-369





George Edward Briggs and John Burdon Sanderson Haldane (1925) A note on the kinetics of enzyme action, Biochem. J., 19: 338-339



# **Briggs-Haldane on Henri-Michaelis-Menten** (only for info. Not needed)

$$E + S \underset{k_{-1}}{\overset{k^1}{\rightleftharpoons}} ES \xrightarrow{k_2} E + P$$

$$\frac{d[ES]}{dt} = k_1[E][S] - k_{-1}[ES] - k_2[ES] = 0$$

$$[ES] = \frac{k_1[E][S]}{k_{-1} + k_2}$$

$$K_m = \frac{k_{-1} + k_2}{k_1}$$

$$[ES] = \frac{[E][S]}{K_m}$$

$$\frac{d[P]}{dt} = k_2[ES]$$

$$[E] = [E_0] - [ES]$$

$$[ES]\frac{K_m}{[S]} = [E_0] - [ES]$$

$$[ES](1 + \frac{K_m}{[S]}) = [E_0]$$

$$[ES] = [E_0] \frac{1}{1 + \frac{K_m}{[S]}}$$

$$\frac{d[P]}{dt} = k_2[E_0] \frac{[S]}{K_m + [S]} = V_{max} \frac{[S]}{K_m + [S]}$$

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$$[E] = [E_0] - [ES]$$

steady-state!!! 
$$[ES]\frac{K_m}{[S]} = [E_0] - [ES]$$

$$[ES] = \frac{k_1[E][S]}{k_{-1} + k_2}$$

$$[ES](1 + \frac{K_m}{[S]}) = [E_0]$$

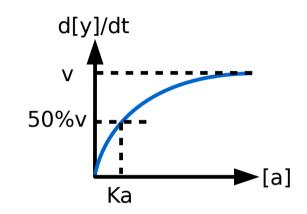
$$K_m = \frac{k_{-1} + k_2}{k_1}$$

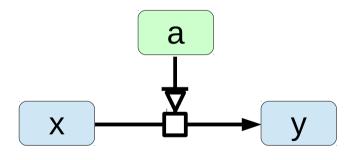
$$[ES] = [E_0] \frac{1}{1 + \frac{K_m}{|S|}}$$

$$[ES] = \frac{[E][S]}{K_m}$$

$$\frac{d[P]}{dt} = k_2[E_0] \frac{[S]}{K_m + [S]} = V_{max} \frac{[S]}{K_m + [S]}$$

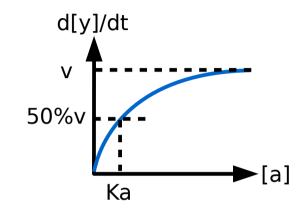
$$\frac{d[y]}{dt} = v(=k \cdot [x])$$

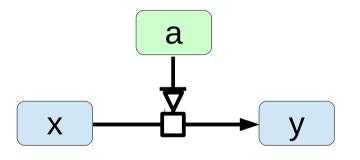




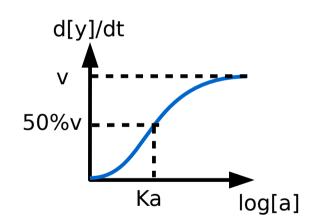
$$\frac{d[y]}{dt} = v \cdot \frac{[a]}{Ka + [a]}$$

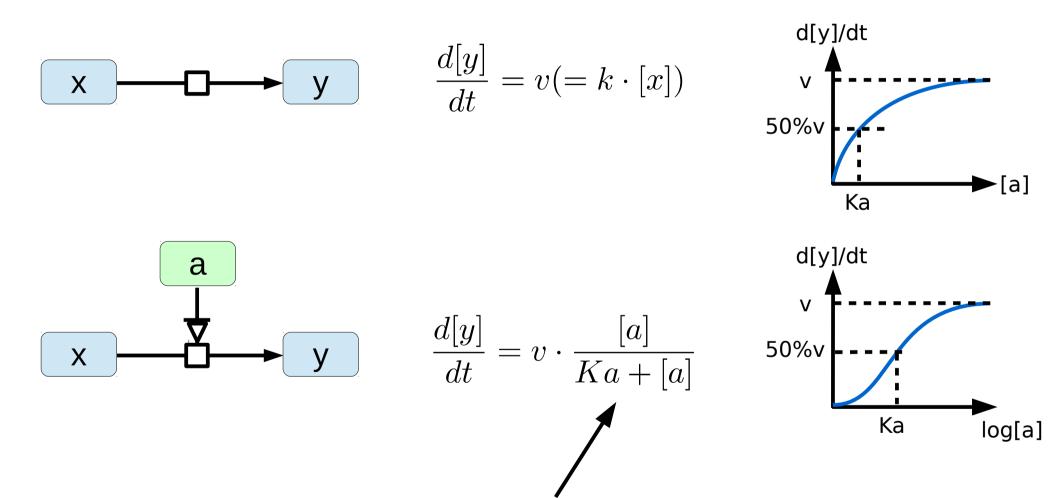
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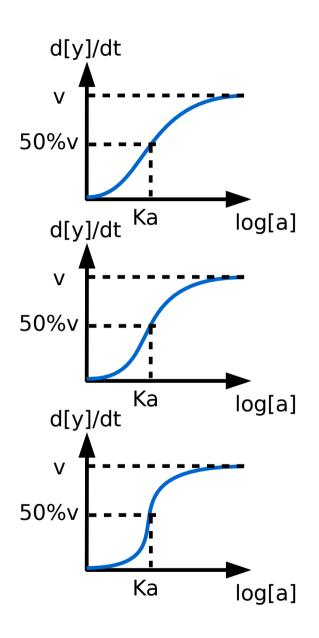
(NB: You can derive that as the fraction of target bound to the activator)

## Phenomenological ultrasensitivity

$$\frac{d[y]}{dt} = v \cdot \frac{[a]}{Ka + [a]}$$

$$\frac{d[y]}{dt} = v \cdot \frac{[a]^2}{Ka^2 + [a]^2}$$

$$\frac{d[y]}{dt} = v \cdot \frac{[a]^n}{Ka^n + [a]^n}$$



The possible effects of the aggregation of the molecules of hæmoglobin on its dissociation curves. By A. V. Hill.

In a previous communication Barcroft and I gave evidence which seemed to us to prove conclusively that dialysed hæmoglobin consists simply of molecules containing each one atom of iron. The molecular weight is therefore Hb = 16,660. These experiments have not been published yet, but I shall assume the results.

Other observers (Reid, Roaf, Hüfner and Gansser) working on different solutions have obtained divergent results. The method used by all of them was the direct estimation of the osmotic pressure, by means of a membrane permeable to salts, but not to hæmoglobin. The method involves a relatively large error, because the quantity measured is small. It is doubtful however whether this can explain the discordant results.

Our work led me to believe that the divergence between the results of different observers was due to an aggregation of the hæmoglobin molecules by the salts present in the solution, a consequent lowering of the number of molecules, and an increase in the average molecular weight as observed by the osmotic pressure method. To test this hypothesis I have applied it to several of the dissociation curves obtained by Barcroft and Camis with hæmoglobin in solutions of various salts, and with hæmoglobin prepared by Bohr's method.

The equation for the reaction would be

$$Hb + O_2 \rightleftharpoons HbO_2$$
,  
 $Hb_n + nO_2 \rightleftharpoons Hb_nO_{2n}$ ,

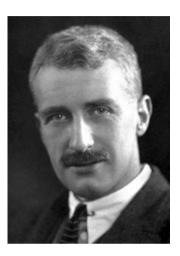
where  $Hb_n$  represents the aggregate of n molecules of Hb. I have supposed that in every solution there are many different sized aggregates, corresponding to many values of n.

If there were in the solution only Hb and Hb<sub>2</sub> the dissociation curve would be

$$y = \lambda \frac{K'x^2}{1 + K'x^2} + (100 - \lambda) \frac{Kx}{1 + Kx}$$
 .....(A),

where  $\lambda^{\circ}/_{0}$  is as Hb<sub>2</sub>,  $(100 - \lambda)^{\circ}/_{0}$  as Hb, K' is the equilibrium constant of the reaction Hb<sub>2</sub> + 2O<sub>2</sub>  $\Longrightarrow$  Hb<sub>2</sub>O<sub>4</sub> and K that of Hb + O<sub>2</sub>  $\Longrightarrow$  HbO<sub>2</sub>: K has the value 125 (Barcroft and Roberts).

Hill (1910) J Physiol 40: iv-vii.



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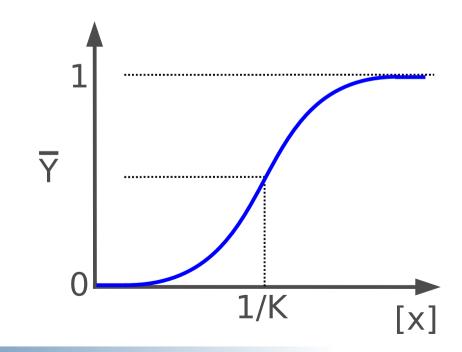
If there were in the solution only Hb and Hb, the dissociation curve would be

$$y = \lambda \frac{K'x^2}{1 + K'x^2} + (100 - \lambda) \frac{Kx}{1 + Kx}$$
 .....(A),

where  $\lambda^{0}/_{0}$  is as Hb<sub>2</sub>,  $(100 - \lambda)^{0}/_{0}$  as Hb, K' is the equilibrium constant of the reaction  $Hb_2 + 2O_2 \rightleftharpoons Hb_2O_4$  and K that of  $Hb + O_2 \rightleftharpoons HbO_3$ : K has the value 125 (Barcroft and Roberts).

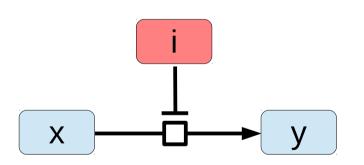
Now it is unlikely that in either of these cases there is only Hb and Hb<sub>2</sub>: and as the calculation of the constants in these equations is very tedious I decided to try whether the equation

$$y = 100 \frac{Kx^n}{1 + Kx^n}$$
 .....(B)

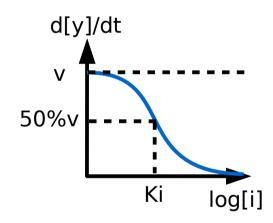


#### **Generalisation: inhibitors**

$$\frac{d[y]}{dt} = v(=k \cdot [x])$$



$$\frac{d[y]}{dt} = v \cdot \frac{Ki^m}{Ki^m + [i]^m}$$



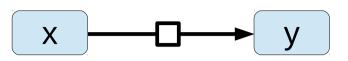


(NB: You can derive that as the fraction of target not bound to the inhibitor)

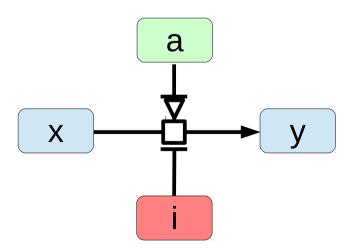
#### Mathematics are beautiful

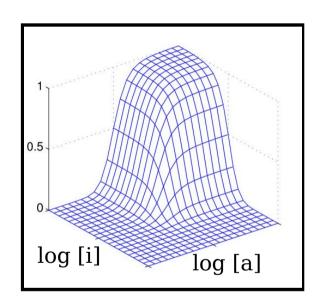
$$1 - \frac{[I]^m}{K_i^m + [I]^m} = \frac{K_1^m}{K_i^m + [I]^m} = \frac{[I]^{-m}}{K_i^{-m} + [I]^{-m}}$$

#### Generalisation: activators and inhibitors



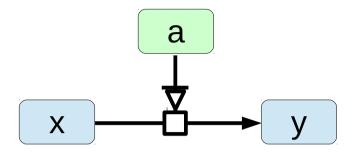
$$\frac{d[y]}{dt} = v(=k \cdot [x])$$



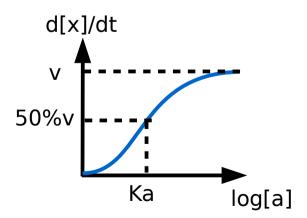


$$\frac{d[y]}{dt} = v \cdot \frac{[a]^n}{Ka^n + [a]^n} \cdot \frac{Ki^m}{Ki^m + [i]^m}$$

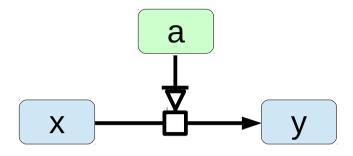
### absolute Vs relative activators



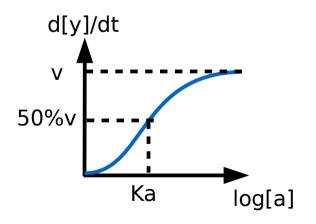
$$\frac{d[y]}{dt} = v \cdot \frac{[a]}{Ka + [a]}$$

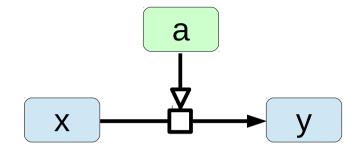


#### absolute Vs relative activators

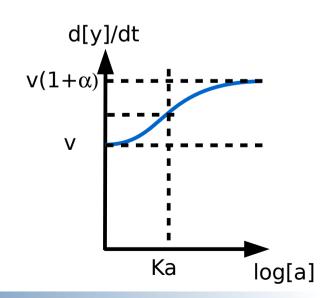


$$\frac{d[y]}{dt} = v \cdot \frac{[a]}{Ka + [a]}$$





$$\frac{d[y]}{dt} = v \cdot (1 + \alpha \cdot \frac{[a]}{Ka + [a]})$$



### 1 compartment

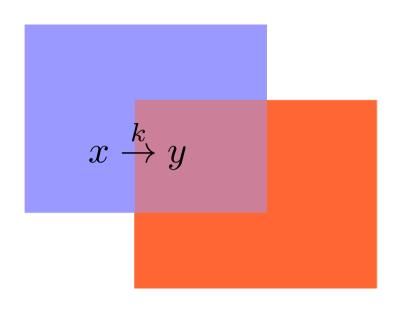
$$x \xrightarrow{k} y$$

$$\frac{d[x]}{dt} = -1 \cdot k \cdot [x]$$

$$\frac{d[y]}{dt} = +1 \cdot k \cdot [x]$$

$$\frac{d[y]}{dt} = +1 \cdot k \cdot [x]$$

### 2 compartments

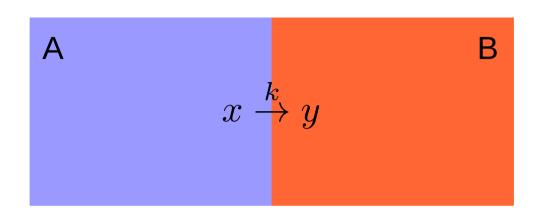


$$\frac{d[x]}{dt} = -1 \cdot k \cdot [x]$$

$$\frac{d[y]}{dt} = +1 \cdot k \cdot [x]$$

$$\frac{d[y]}{dt} = +1 \cdot k \cdot [x]$$

## 2 compartments



$$\frac{d[x]_A}{dt} = -1 \cdot k \cdot [x]_A$$

$$\frac{d[y]_B}{dt} = +1 \cdot k \cdot [x]_A$$

$$nx_A = -1 \cdot k \cdot [x]_A \cdot V_A$$

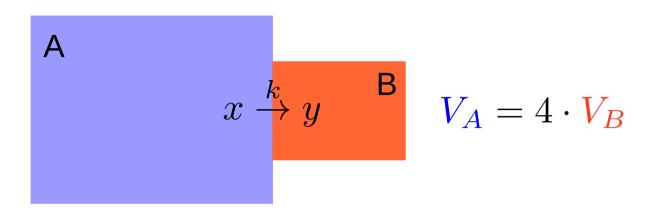
$$ny_B = +1 \cdot k \cdot [x]_A \cdot V_B$$

$$V_A = V_B \Rightarrow nx_A = ny_B$$

A 
$$x \stackrel{k}{\rightarrow} y$$
 B  $V_A = 4 \cdot V_B$ 

$$\frac{d[x]_A}{dt} = -1 \cdot k \cdot [x]_A$$

$$\frac{d[y]_B}{dt} = +1 \cdot k \cdot [x]_A$$



$$\frac{d[x]_A}{dt} = -1 \cdot k \cdot [x]_A$$

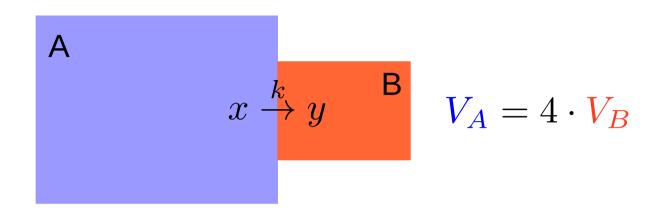
$$\frac{d[y]_B}{dt} = +1 \cdot k \cdot [x]_A$$

$$nx_A = -1 \cdot k \cdot [x]_A \cdot V_A$$

$$ny_B = +1 \cdot k \cdot [x]_A \cdot V_B$$

$$nx_A = 4 \cdot ny_B$$

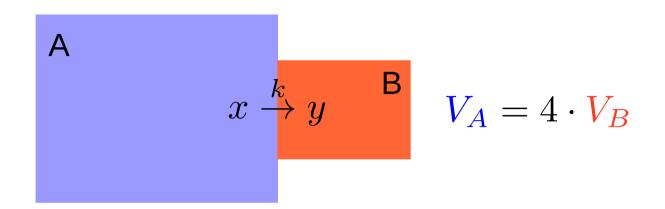




$$\frac{d[x]_A}{dt} = -1 \cdot k \cdot [x]_A \cdot \frac{V_A}{V_A} \qquad nx_A = k \cdot [x]_A \cdot \frac{V_A}{V_A} \cdot V_A$$

$$\frac{d[y]_B}{dt} = +1 \cdot k \cdot [x]_A \cdot \frac{V_A}{V_B} \qquad ny_B = k \cdot [x]_A \cdot \frac{V_A}{V_B} \cdot V_B$$

$$nx_A = k \cdot [x]_A \cdot \frac{V_A}{V_A} \cdot V_A$$
 $ny_B = k \cdot [x]_A \cdot \frac{V_A}{V_B} \cdot V_B$ 

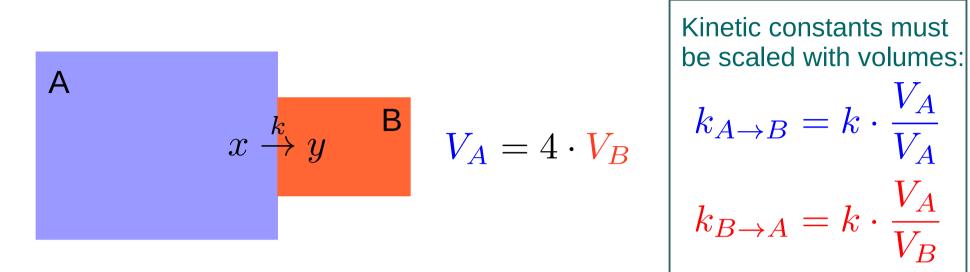


$$\begin{split} \frac{d[x]_A}{dt} &= -1 \cdot k \cdot [x]_A \cdot \frac{V_A}{V_A} & nx_A = k \cdot [x]_A \cdot \frac{V_A}{V_A} \cdot \mathcal{Y}_A \\ \frac{d[y]_B}{dt} &= +1 \cdot k \cdot [x]_A \cdot \frac{V_A}{V_B} & ny_B = k \cdot [x]_A \cdot \frac{V_A}{V_B} \cdot \mathcal{Y}_B \end{split}$$

$$\frac{a[x]_A}{dt} = -1 \cdot k \cdot [x]_A \cdot \frac{V_A}{V_A} \qquad nx_A = k \cdot [x]_A \cdot \frac{V_A}{V_A} \cdot Y_A$$

$$\frac{d[y]_B}{dt} = +1 \cdot k \cdot [x]_A \cdot \frac{V_A}{V_B} \qquad ny_B = k \cdot [x]_A \cdot \frac{V_A}{V_B} \cdot Y_B$$

$$nx_A = ny_B$$



$$k_{A \to B} = k \cdot \frac{V_A}{V_A}$$

$$k_{B \to A} = k \cdot \frac{V_A}{V_B}$$

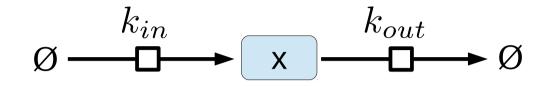
$$\begin{split} \frac{d[x]_A}{dt} &= -1 \cdot k \cdot [x]_A \cdot \frac{V_A}{V_A} & nx_A = k \cdot [x]_A \cdot \frac{V_A}{V_A} \cdot V_A \\ \frac{d[y]_B}{dt} &= +1 \cdot k \cdot [x]_A \cdot \frac{V_A}{V_B} & ny_B = k \cdot [x]_A \cdot \frac{V_A}{V_B} \cdot V_B \end{split}$$

$$\frac{a[x]_A}{dt} = -1 \cdot k \cdot [x]_A \cdot \frac{V_A}{V_A} \qquad nx_A = k \cdot [x]_A \cdot \frac{V_A}{V_A} \cdot Y_A$$

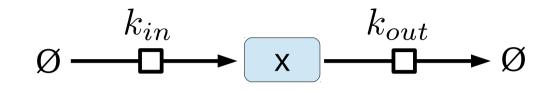
$$\frac{d[y]_B}{dt} = +1 \cdot k \cdot [x]_A \cdot \frac{V_A}{V_B} \qquad ny_B = k \cdot [x]_A \cdot \frac{V_A}{V_B} \cdot Y_B$$

$$nx_A = ny_B$$

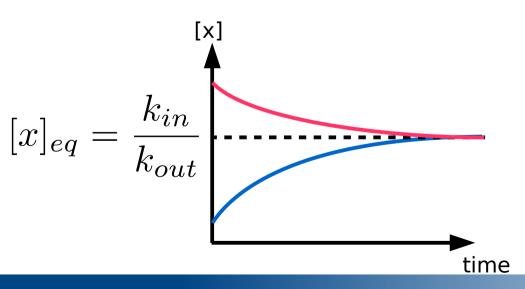


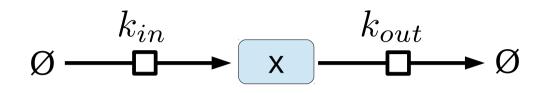


$$\frac{d[x]}{dt} = k_{in} - k_{out} \cdot [x]$$

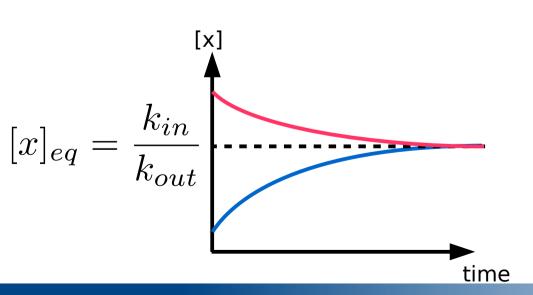


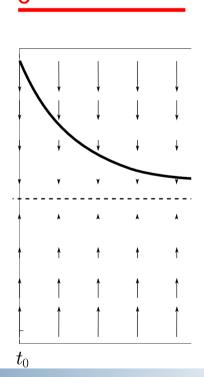
$$\frac{d[x]}{dt} = k_{in} - k_{out} \cdot [x]$$





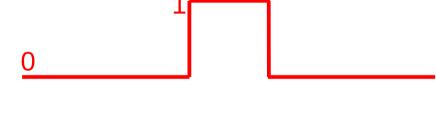
$$\frac{d[x]}{dt} = k_{in} - k_{out} \cdot [x]$$

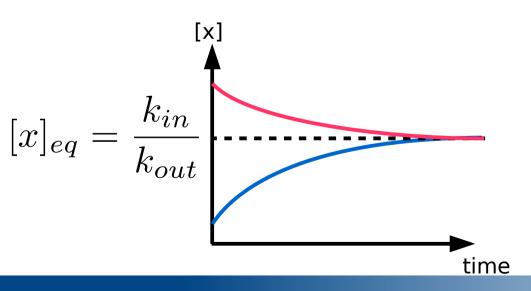


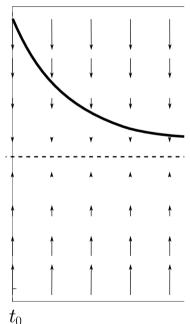


$$\emptyset \xrightarrow{k_{in}} x \xrightarrow{k_{out}} \emptyset$$

$$\frac{d[x]}{dt} = k_{in} - k_{out} \cdot [x] - k_{pert} \cdot [x]$$

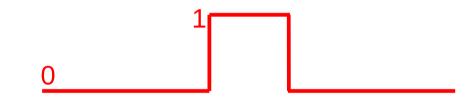


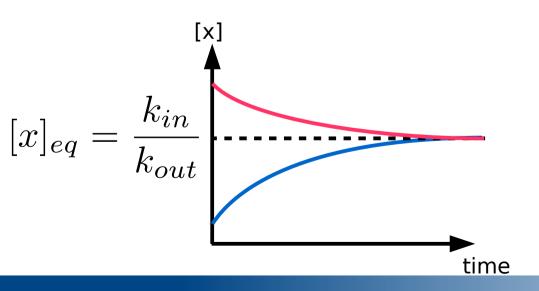


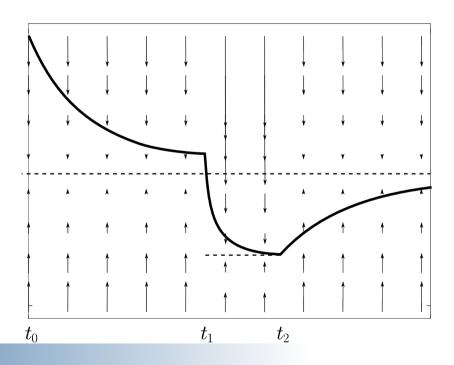


$$\varnothing \xrightarrow{k_{in}} x \xrightarrow{k_{out}} \varnothing$$

$$\frac{d[x]}{dt} = k_{in} - k_{out} \cdot [x] - k_{pert} \cdot [x]$$

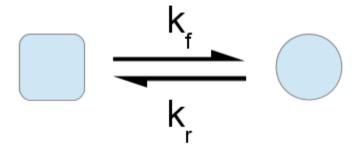




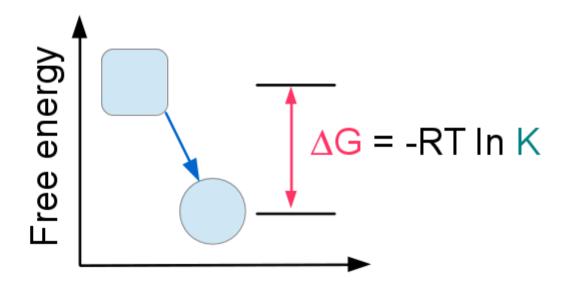


Questions?

### **Conformational equilibrium**



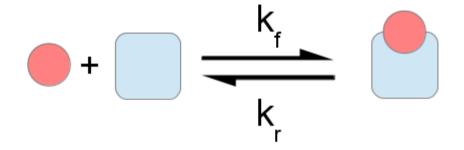
$$K = \frac{\begin{bmatrix} \\ \\ \end{bmatrix}}{\begin{bmatrix} \\ \end{bmatrix}} = \frac{k_r}{k_f}$$



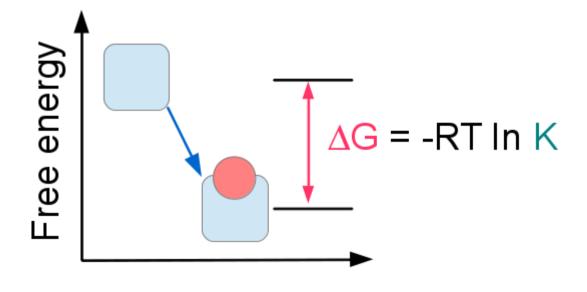
$$K < 1$$
  $\longrightarrow$   $K_f > K_r$ 

$$\Delta G > 0$$
Shift towards

### **Binding equilibrium**

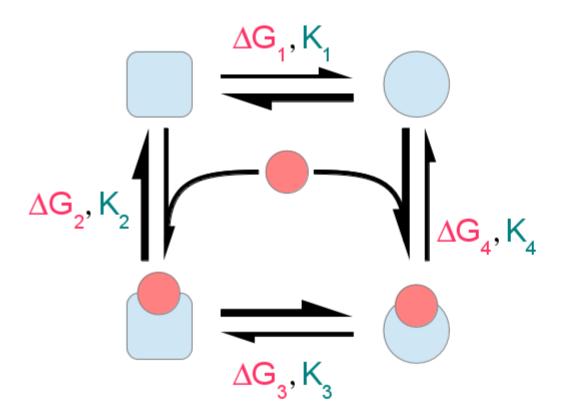


$$K = \frac{\begin{bmatrix} \\ \end{bmatrix} \begin{bmatrix} \\ \end{bmatrix} \end{bmatrix}}{\begin{bmatrix} \\ \end{bmatrix}} = \frac{k_r}{k_f}$$

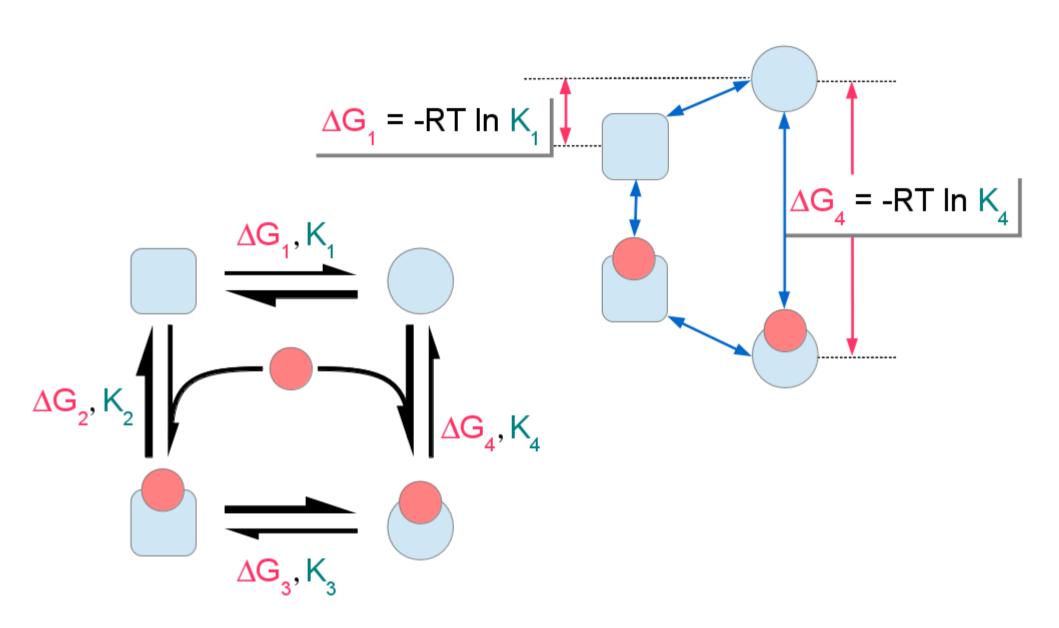


$$K < 1$$
  $\longrightarrow$   $\Delta G > 0$  Shift towards

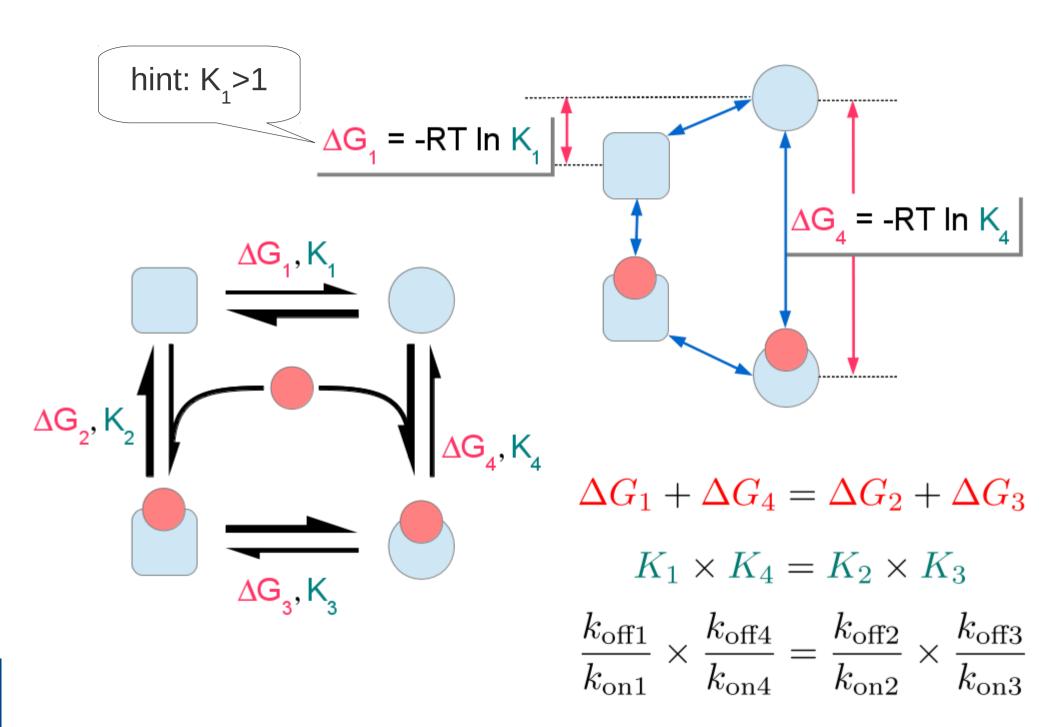
### How does a ligand activate its target?



### How does a ligand activate its target?



## How does a ligand activate its target?



## Add energies

# Multiply constants

+1 quantum energy = constant divided by 10

Explore constants exponentially:

